

## Use of the binary interaction parameter $L_{ij}(T, P, x_i)$ function for van der Waals-type equations of state in vapor–liquid equilibrium calculations

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### Abstract

The predictive accuracy of the newly developed binary interaction parameter function  $L_{ij} = L_{ij}(T, P, x_i)$  of Lielmezs and co-workers has been studied further by means of the Redlich–Kwong–Soave (RKS) and Peng–Robinson (PR) equations of state in the vapor–liquid equilibria calculations over a wide range of  $P$ – $T$ – $x$ – $y$  values. Sets of coefficients for use in the binary interaction parameter function  $L_{ij} = L_{ij}(T, P, x_i)$  have been established for 29 selected binary systems.

The results calculated of the vapor–liquid equilibria (bubble point) for the binary systems considered (L-RKS, L-PR) are in excellent agreement with the experimental data and the values obtained using the  $F$ -function of two-parameter cubic equations of state (F-RKS, F-PR). The predictions made in this work (L-RKS, L-PR) have a slight edge over the results calculated via the original Redlich–Kwong–Soave (RKS) and Peng–Robinson (PR) methods.

### LIST OF SYMBOLS

$a, b$	parameters of cubic equation of state
$e, f, g, h$	dimensionless coefficients of eqn. (9)
F-RKS	$F$ -function modification of RKS equation of state with $L_{ij}$ -function [15]
F-PR	$F$ -function modification of PR equation of state with $L_{ij}$ -function [15]
$k_{ij}$	binary interaction parameter for RKS and PR equations of state
$L_{ij}$	binary interaction parameter for L-RKS and L-PR equations of state
L-RKS	RKS equation with $L_{ij}$ -function

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L-PR	PR equation with $L_{ij}$ -function
$N$	number of data points
$P$	pressure
PR	Peng–Robinson equations of state [3]
RKS	Redlich–Kwong–Soave equation of state
$R$	universal gas constant
$T$	temperature
$x$	composition of liquid phase
$y$	composition of vapor phase

### Subscripts

$c$	critical state
$i, j$	components of mixture
$m$	mixture

### INTRODUCTION

The generalized cubic equation of state of van der Waals type can be expressed as

$$P = \frac{RT}{V - b} - \frac{a}{V^2 + uV + wb^2} \quad (1)$$

where  $u$  and  $w$  must satisfy the constraints [1]

$$w > -u - 1 \quad \text{for } u \geq -2$$

$$w > \frac{u^2}{4} \quad \text{for } u \leq -2 \quad (2)$$

For the Redlich–Kwong–Soave (RKS) equation [2],  $u = 1$  and  $w = 0$ ; for the Peng–Robinson (PR) equation [3],  $u = 2$  and  $w = 1$ .

Following the well-known one-fluid model of van der Waals, we write the mixing rules as

$$a_m = \sum_i \sum_j x_i x_j (a_i a_j)^{1/2} (1 - k_{ij}) \quad (3)$$

$$b_m = \sum_i x_i b_i \quad (4)$$

It has been common practice to assume that the binary interaction parameter  $k_{ij}$  (eqn. (3)) is independent of the thermodynamic state properties, i.e. temperature  $T$ , pressure  $P$  and composition  $x$  [4–8]. In

recent years, some attempts have been made to correlate  $k_{ij}$  with temperature  $T$  [9–11]. Recently, following Lielmezs' work [12, 13], we successfully introduced, instead of the fixed optimum binary interaction parameter  $L_{ij} = 1 - k_{ij}$ , a state-dependent interaction parameter function  $L_{ij}(T, P, x_i)$  into the  $F$ -function modification of the RKS and PR equations of state, F-RKS and F-PR [14–15]. In this work, we test directly the applicability of the  $L_{ij}$ -function to the original RKS and PR equations of state, denoted in this work as L-RKS and L-PR over a wide range of  $P$ - $T$ - $x$ - $y$  data. To do this, experimental data of twenty-nine binary systems were selected from a number of sources. These literature data were considered of sufficient reliability so no further evaluation of their accuracy was made. The constants needed to perform the vapor–liquid equilibrium calculations,  $T_c$ ,  $P_c$  and the acentric factor  $\omega$  values, were taken from our previous work [14].

The calculations of the bubble-point pressure and vapor mole fractions were performed in two ways: first, via the  $L_{ij}$ -function in conjunction with the RKS and PR equations of state, identified as L-RKS and L-PR; and second, by means of the fixed averaged optimum binary interaction parameter  $k_{ij}$  ( $k_{ij} = 1 - L_{ij}$ ), which is independent of thermodynamic state. Following our previous work [15], the optimum binary interaction parameter  $L_{ij}$  or  $k_{ij}$  values were established by means of an objective function given as

$$SP = \frac{100}{N} \sum_i^N \left( \left| \frac{P_{\text{cal}} - P_{\text{exp}}}{P_{\text{exp}}} \right|_i + |y_{\text{cal}} - y_{\text{exp}}|_i \right) \quad (5)$$

An optimum  $L_{ij}$  or  $k_{ij}$  value is the one that minimizes the objective function  $SP$  over the same set of experimental data.

The accuracy of the bubble point calculations is determined with reference to experimental data by means of the relative deviation of pressure  $\Delta P$  (%) and the absolute deviation of vapor mole fraction  $\Delta y$ , defined as

$$\Delta P (\%) = \frac{1}{N} \sum_i \left| \frac{P_{\text{cal}} - P_{\text{exp}}}{P_{\text{exp}}} \right|_i \times 100 \quad (6)$$

$$\Delta y = \frac{1}{N} \sum_i |y_{\text{cal}} - y_{\text{exp}}|_i \times 100 \quad (7)$$

All results calculated were compared to the experimental data and the values obtained by means of the original Redlich–Kwong–Soave (RKS) and Peng–Robinson (PR) equations.

#### BINARY INTERACTION PARAMETER FUNCTION $L_{ij}(T, P, x_i)$

It is commonly assumed that the binary interaction parameter  $L_{ij}$  (or  $k_{ij}$ ) is a characteristic constant of a given binary system and, as such, is

TABLE 1

The results of bubble point calculations for the CO<sub>2</sub>–methanol system [38] using optimum  $L_{12}$  values and the  $L_{12}$ -function

No.	$T/K$	$P/\text{atm}$	$x_1$	$L_{12}$ (optimum)	$\Delta P/(\%)$	$\Delta y_1$	$L_{12}$ (function)	$\Delta P/(\%)$	$\Delta y_1$
1	298.15	7.792	0.0596	0.97241	1.0158	0.218	0.97212	1.6433	0.280
2	298.15	18.814	0.1548	0.97039	0.0078	0.063	0.96835	1.5462	0.050
3	298.15	30.246	0.2601	0.96531	0.0024	0.065	0.96406	0.8698	0.070
4	298.15	39.503	0.3495	0.95671	0.0083	0.041	0.96024	2.0873	0.040
5	298.15	48.664	0.4886	0.95000	0.0010	0.035	0.95392	1.7272	0.040
6	298.15	55.013	0.6451	0.92648	0.0003	0.055	0.94620	4.5184	0.010
7	298.15	57.509	0.7685	0.86238	0.0004	0.319	0.93983	6.7092	0.000
8	298.15	58.749	0.9002	0.75789	2.2090	1.107	0.93316	4.5968	0.030
9	313.15	5.697	0.0285	0.96735	0.0084	0.260	0.95275	3.7643	0.040
10	313.15	17.469	0.1023	0.95751	0.0053	0.026	0.95028	5.3381	0.060
11	313.15	29.654	0.1641	0.94351	0.0011	0.067	0.94815	3.2101	0.090
12	313.15	40.337	0.2339	0.94256	0.0027	0.063	0.94565	2.1049	0.070
13	313.15	56.313	0.3655	0.94188	0.0064	0.153	0.94061	0.7757	0.160
14	313.15	61.903	0.4201	0.93967	0.0004	0.184	0.93835	0.7353	0.190
15	313.15	70.006	0.5429	0.93590	0.0038	0.226	0.93282	1.3053	0.270
16	313.15	76.021	0.6892	0.92412	2.8372	0.198	0.92542	3.0660	0.180
17	313.15	79.53	0.897	0.91684	5.5832	0.669	0.91464	5.5928	0.650

independent of thermodynamic state. Indeed, the fluid phase equilibria of many binary systems can be described with reasonable accuracy using fixed optimum  $k_{ij}$  or  $L_{ij}$  values, for instance, in conjunction with the RKS and PR equations of state [16]. However recent work has shown [12–15] that any small change in the  $k_{ij}$  or  $L_{ij}$  values may significantly affect prediction of the fluid phase behavior and that thermodynamic-state-dependent binary interaction parameter ( $k_{ij}$  or  $L_{ij}$ ) functions may need to be introduced instead.

This need is illustrated in Table 1 and Fig. 1. Table 1 lists the fixed optimum  $L_{ij}$  values and  $L_{ij}$ -function values, calculated from the RKS equation for each individual experimental point of the CO<sub>2</sub>–CH<sub>3</sub>OH binary mixture. Figure 1, (a) and (b), show the fixed optimum  $L_{ij}$  values and the  $L_{ij}$ -function values, respectively, calculated from the RKS equation plotted against pressure  $P$  and liquid-phase composition  $x$  at constant temperature  $T$  for the ethane– $n$ -hexane and methane– $n$ -decane binary systems. Figure 1(c) shows the fixed optimum  $L_{ij}$  and  $L_{ij}$ -function values obtained via the RKS equation plotted against temperature  $T$  and liquid-phase composition  $x$  at constant pressure  $P$  for the methane– $n$ -decane binary system.

Table 1 and Fig. 1(a)–(c) strengthen the observation [12–15] that the binary interaction parameter  $L_{ij}$  (or  $k_{ij}$ ) can be considered as a complex

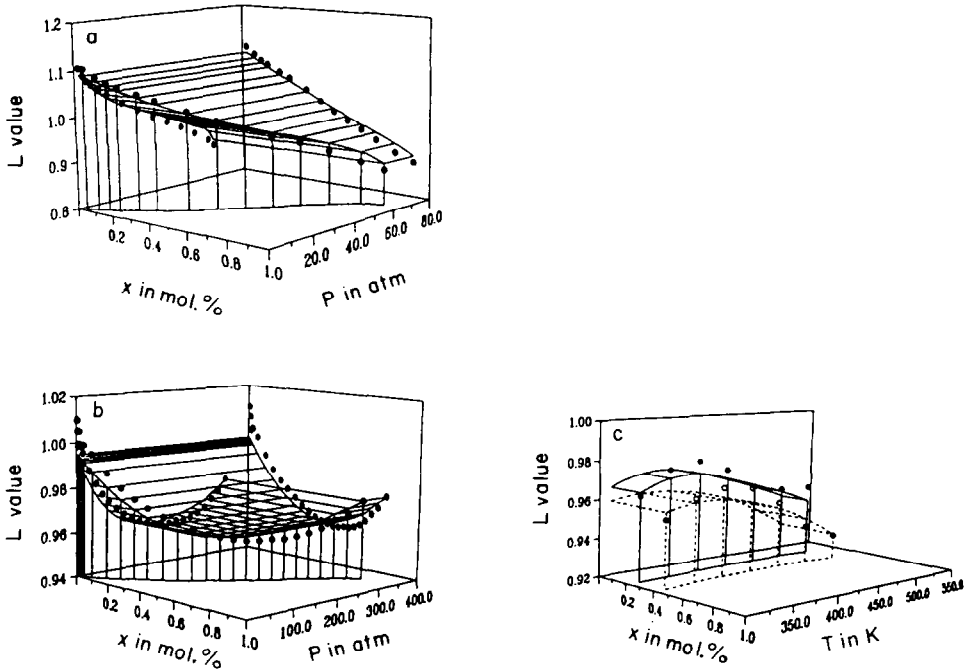


Fig. 1. (a), (b)  $L$ -value vs. mole fraction and pressure at constant temperature: ●, optimum  $L$ -value; —,  $L_{ij}$ -function for (a) the ethane- $n$ -hexane system at  $T = 338.7$  K, and (b) the methane- $n$ -decane system at  $T = 344.26$  K. (c)  $L$ -value vs. mole fraction and temperature at constant pressure for the methane- $n$ -decane system: ●, optimum  $L$ -value; —,  $L_{ij}$ -function, at  $P = 54.5$  atm; ○, optimum  $L$ -value; ···,  $L_{ij}$ -function at  $P = 119.0$  atm.

function of the thermodynamic state, i.e.  $L_{ij} = L_{ij}(T, P, x_i)$  or  $k_{ij} = k_{ij}(T, P, x_i)$ .

The linear form of the  $L_{ij}$  (or  $k_{ij}$ ) function can be obtained by expanding the thermodynamic-state dependency of the  $L_{ij}$ -function,  $L_{ij}(T, P, x_i)$ , into MacLaurin's series truncated to the first-order term, i.e.

$$L_{ij}(T, P, x_i) = L_{ij}^o + \frac{\partial L_{ij}}{\partial x_i} x_i + \frac{\partial L_{ij}}{\partial P} P + \frac{\partial L_{ij}}{\partial T} T \tag{8}$$

Following Lielmezs [12, 13], we identify

$$L_{ij}^o = e_{ij} \quad \frac{\partial L_{ij}}{\partial x_i} = f_{ij} \quad \frac{\partial L_{ij}}{\partial P} = g_{ij} \quad \frac{\partial L_{ij}}{\partial T} = h_{ij} \tag{8a}$$

Putting eqn. (8a) into eqn. (8), we obtain

$$L_{ij}(T, P, x_i) = e_{ij} + f_{ij}x_i + g_{ij}P + h_{ij}T \tag{9}$$

with coefficients  $e_{ij}$ ,  $f_{ij}$ ,  $g_{ij}$  and  $h_{ij}$  are characteristic dimensionless constants of a given binary system [12–15].

To satisfy the requirement that  $L_{ij} = 1$  and  $L_{ji} = L_{ij}$ , we set [15]

$$\begin{aligned} e_{ii} &= 1 & f_{ii} &= 0 & g_{ii} &= 0 & h_{ii} &= 0 \\ e_{ji} &= e_{ij} & f_{ji} &= \frac{x_i}{x_j} f_{ij} & g_{ji} &= g_{ij} & h_{ji} &= h_{ij} \end{aligned} \quad (10)$$

Putting the  $L_{ij}$ -function (eqn. (9)) into the mixing rule (eqn. (3)) for the RKS and PR equations of state, we obtain the L-RKS and L-PR equations. (For the derivation of the F-RKS and F-PR equations, see refs. 14, 15.) The values of coefficients  $e_{ij}$ ,  $f_{ij}$ ,  $g_{ij}$  and  $h_{ij}$  of the L-RKS and L-PR equations were determined by a method similar to that outlined in our previous work regarding the F-RKS and F-PR equations [15]. The values of the coefficients  $e_{ij}$ ,  $f_{ij}$ ,  $g_{ij}$  and  $h_{ij}$  (eqn. (9)) obtained for the L-RKS and L-PR equations for all 29 binary systems tested in this work are listed below in Table 3.

The vapor–liquid equilibria (bubble point) results calculated by means of the L-RKS and L-PR equations for all binary systems considered are in excellent agreement with the experimental data, and with the values obtained using the  $F$ -function of two-parameter cubic equations of state (F-RKS, F-PR [14, 15], and show a slight edge over the original RKS and PR equations (see discussion below).

## RESULTS AND DISCUSSION

The introduction of the linearized  $L_{ij}$ -function (eqn. (9)) into the mixing rule (eqn. (3)) for calculating vapor–liquid equilibria has established a simple and reliable method (L-RKS, L-PR) needing nearly the same computer time as the original RKS and PR equations of state. The  $L_{ij}$ -function (eqn. (9)) was used only to provide better  $L_{ij}$  values for every point tested; it was not directly introduced into the equation of state (eqn. (1)) to derive the fugacity coefficient expression (see Appendix of ref. 15).

The bubble point calculations presented were performed following our previous work [15]. First, an initial  $P$  value was assumed; then, from this initial  $P$ , an initial  $L_{ij}$  value was obtained using (eqn. (9)), and the iteration process started. The iteration process was repeated until a preset convergence limit was reached [15].

Table 4 compares the results of the bubble point calculations performed by means of the L-RKS and L-PR equations (Table 3), the results using the original RKS and PR equations with the fixed averaged optimum  $k_{ij}$  values (Table 2) and the results obtained using the  $F$ -function of the two-parameter cubic equation, the F-RKS and F-PR equations, taken from ref. 15.

The fixed averaged optimum binary interaction parameter  $k_{ij}$  values (Table 2) were determined by minimizing the objective function SP (eqn. (5)) over all data points for a given system.

Figures 2 and 3 compare the results obtained by the methods considered

TABLE 2

Fixed optimum values of the binary interaction parameter  $k_{12}$  for use in the RKS and PR methods.<sup>a</sup>

System	Ref.	T range/ K	P range/ atm	Number of data points	$k_{12}$	
					RKS	PR
CH <sub>4</sub> -C <sub>2</sub> H <sub>6</sub>	17	144–200	1–51	126	-0.02404	0.0
CH <sub>4</sub> -C <sub>3</sub> H <sub>8</sub>	18	277–361	6–100	99	0.02519	0.02628
CH <sub>4</sub> - <i>n</i> -C <sub>4</sub> H <sub>10</sub>	19	294–394	2–131	123	0.02418	0.02959
CH <sub>4</sub> - <i>n</i> -C <sub>6</sub> H <sub>14</sub>	20	298–423	10–120	51	0.03441	0.03790
CH <sub>4</sub> - <i>n</i> -C <sub>8</sub> H <sub>18</sub>	21	298–423	10–70	33	0.04571	0.04231
CH <sub>4</sub> - <i>n</i> -C <sub>10</sub> H <sub>22</sub>	22	310–511	1–357	156	0.03479	0.03797
C <sub>2</sub> H <sub>6</sub> -C <sub>3</sub> H <sub>8</sub>	23	310–344	12–51	49	-0.00341	-0.00325
C <sub>2</sub> H <sub>6</sub> - <i>n</i> -C <sub>5</sub> H <sub>12</sub>	24	277–411	0–67	66	0.00553	0.00869
C <sub>2</sub> H <sub>6</sub> - <i>n</i> -C <sub>6</sub> H <sub>14</sub>	25	338–450	0–78	42	-0.02566	-0.02790
C <sub>2</sub> H <sub>6</sub> - <i>n</i> -C <sub>8</sub> H <sub>18</sub>	26	313–373	4–52	46	0.01744	0.01877
CH <sub>4</sub> -CO <sub>2</sub>	27	209–271	14–78	42	0.10378	0.10088
CO <sub>2</sub> -C <sub>2</sub> H <sub>6</sub>	28	223–293	5–62	65	0.13682	0.12757
C <sub>3</sub> H <sub>8</sub> -CO <sub>2</sub>	29	244–267	5–26	21	0.13438	0.12950
CO <sub>2</sub> - <i>n</i> -C <sub>4</sub> H <sub>10</sub>	30	310–378	3–74	54	0.14267	0.13632
CO <sub>2</sub> - <i>n</i> -C <sub>5</sub> H <sub>12</sub>	31	252–459	1–95	108	0.12934	0.11916
CO <sub>2</sub> - <i>n</i> -C <sub>6</sub> H <sub>14</sub>	32	313–393	7–114	39	0.13937	0.12717
CO <sub>2</sub> - <i>n</i> -C <sub>10</sub> H <sub>22</sub>	33	277–511	2–186	97	0.12475	0.10929
CH <sub>4</sub> -H <sub>2</sub> S	43	277–344	11–133	62	0.08266	0.08273
C <sub>2</sub> H <sub>6</sub> -H <sub>2</sub> S	34	200–283	1–30	43	0.08573	0.08264
H <sub>2</sub> S-C <sub>3</sub> H <sub>8</sub>	35	217–344	1–27	41	0.08502	0.08207
H <sub>2</sub> S- <i>n</i> -C <sub>5</sub> H <sub>12</sub>	36	277–411	0–89	55	0.08407	0.07214
H <sub>2</sub> S- <i>n</i> -C <sub>10</sub> H <sub>22</sub>	37	277–444	1–132	55	0.04529	-0.10002
CO <sub>2</sub> -methanol	38	298–313	5–80	17	0.02356	0.05277
Acetone-CO <sub>2</sub>	39	298–313	4–73	25	0.00644	0.01073
Acetone-methanol	40	373–473	3–39	39	-0.00491	-0.00378
Acetone-H <sub>2</sub> O	40	373–523	3–67	69	-0.12428	-0.12335
Methanol-H <sub>2</sub> O	40	373–523	1–84	56	-0.08116	-0.08131
Ethanol-H <sub>2</sub> O	41	423–623	5–187	85	-0.08528	-0.08344
NH <sub>3</sub> -H <sub>2</sub> O	42	333–420	0–16	63	-0.28314	-0.26532

<sup>a</sup> Apart from the CH<sub>4</sub>-*n*-C<sub>10</sub>H<sub>12</sub>, CO<sub>2</sub>-*n*-C<sub>5</sub>H<sub>22</sub>, CO<sub>2</sub>-*n*-C<sub>10</sub>H<sub>22</sub>, C<sub>2</sub>H<sub>6</sub>-H<sub>2</sub>S, and H<sub>2</sub>S-*n*-C<sub>10</sub>H<sub>22</sub> systems, all the  $k_{12}$  values were taken from our previous work [15].

in this work. Both Table 4 and Figs. 2 and 3 show that the L-RKS and L-PR equations predict with high accuracy the vapor-liquid equilibrium for all systems tested. Table 4 shows that for hydrocarbon-hydrocarbon, CO<sub>2</sub>-hydrocarbon and H<sub>2</sub>S-hydrocarbon binary systems, the predictive accuracy hardly differs between the F-RKS and L-RKS, and F-PR and L-PR calculation methods. However, the polar-polar mixtures such as CH<sub>3</sub>OH-H<sub>2</sub>O, C<sub>2</sub>H<sub>5</sub>OH-H<sub>2</sub>O and NH<sub>3</sub>-H<sub>2</sub>O, the F-RKS and F-PR methods predict more accurately than the L-RKS and L-PR methods.

TABLE 3

Coefficients of the function  $L_{11} = e_{12} + f_{12}x_1 + g_{12}P + h_{12}T$  (eqn. (9)) for use in the L-RKS and L-PR methods

System	L-RKS				L-PR			
	$e_{12}$	$f_{12} \times 10$	$g_{12} \times 10^2$	$h_{12} \times 10^3$	$e_{12}$	$f_{12} \times 10$	$g_{12} \times 10^2$	$h_{12} \times 10^3$
CH <sub>4</sub> -C <sub>2</sub> H <sub>6</sub>	0.95678	0.20630	-0.03228	0.25792	0.97502	0.02820	-0.01453	0.14203
CH <sub>4</sub> -C <sub>3</sub> H <sub>8</sub>	0.96575	2.69301	-0.18347	0.10858	0.77294	4.80360	-0.31277	0.78981
CH <sub>4</sub> -n-C <sub>4</sub> H <sub>10</sub>	0.99214	2.84307	-0.13978	-0.03766	0.90420	3.68099	-0.17669	0.22783
CH <sub>4</sub> -n-C <sub>6</sub> H <sub>14</sub>	1.27305	-5.70018	0.21552	-0.92034	1.17254	-3.73739	0.14366	-0.63260
CH <sub>4</sub> -n-C <sub>8</sub> H <sub>18</sub>	1.11264	-5.35230	0.22497	-0.49815	1.04113	-3.53205	0.15731	-0.29240
CH <sub>4</sub> -n-C <sub>10</sub> H <sub>22</sub>	1.04558	-1.67465	0.03516	-0.16053	1.04812	-2.64264	0.05582	-0.15242
C <sub>2</sub> H <sub>6</sub> -n-C <sub>3</sub> H <sub>8</sub>	0.72721	0.82969	-0.25168	0.99842	1.14515	-0.23852	-0.00310	-0.41566
C <sub>2</sub> H <sub>6</sub> -n-C <sub>5</sub> H <sub>12</sub>	1.02175	0.03561	-0.03726	-0.06636	1.02775	-0.05579	-0.03207	-0.08875
C <sub>2</sub> H <sub>6</sub> -n-C <sub>6</sub> H <sub>14</sub>	1.63388	-3.28189	0.08754	-1.52848	1.38630	-2.96431	0.04223	-0.79208
C <sub>2</sub> H <sub>6</sub> -n-C <sub>8</sub> H <sub>18</sub>	0.98776	0.16048	-0.03105	-0.01241	0.98791	0.03148	-0.01343	-0.01453
CH <sub>4</sub> -CO <sub>2</sub>	1.13181	-0.88547	0.03905	-0.97922	0.97457	0.07887	0.00875	-0.35275
CO <sub>2</sub> -C <sub>2</sub> H <sub>6</sub>	0.71901	0.14449	-0.09018	0.62547	0.85087	0.10031	0.02102	0.02498
C <sub>3</sub> H <sub>8</sub> -CO <sub>2</sub>	0.85142	-0.31832	-0.08408	0.17137	0.85780	-0.24547	-0.06211	0.13545
CO <sub>2</sub> -n-C <sub>4</sub> H <sub>10</sub>	0.86740	0.66946	-0.06727	-0.02491	0.88476	0.31487	-0.01971	-0.06519
CO <sub>2</sub> -n-C <sub>5</sub> H <sub>12</sub>	0.82959	0.48544	-0.04625	0.13727	0.82262	0.41132	-0.04028	0.19084
CO <sub>2</sub> -n-C <sub>6</sub> H <sub>14</sub>	0.89448	0.53183	-0.01009	-0.13630	0.84932	0.89857	-0.03312	0.02710
CO <sub>2</sub> -n-C <sub>10</sub> H <sub>22</sub>	0.85965	0.18911	0.00758	0.00226	0.85092	0.42523	-0.00591	0.06351
CH <sub>4</sub> -H <sub>2</sub> S	0.91136	2.77753	-0.07310	0.05526	0.91136	2.77753	-0.07310	0.05526
C <sub>2</sub> H <sub>6</sub> -H <sub>2</sub> S	0.90915	-0.08189	0.00688	0.02888	0.94067	-0.14024	0.03764	-0.09888
H <sub>2</sub> S-C <sub>3</sub> H <sub>8</sub>	0.85137	0.34481	-0.01858	0.18752	0.91210	0.41049	-0.04321	-0.04321
H <sub>2</sub> S-n-C <sub>3</sub> H <sub>12</sub>	0.89305	0.56079	-0.09912	0.12477	0.91044	0.26112	-0.04373	0.10172
H <sub>2</sub> S-n-C <sub>10</sub> H <sub>22</sub>	0.87430	0.76052	-0.10508	0.26097	0.86116	0.75622	-0.12541	0.29363
CO <sub>2</sub> -methanol	1.38707	-0.52619	0.01090	-1.38403	1.40858	-1.52728	0.08727	-1.46565
Acetone-CO <sub>2</sub>	1.13300	0.53069	0.07482	-0.62326	1.15952	1.10006	0.15253	-0.89983
Acetone-methanol	1.07747	-0.61707	-0.05404	-0.08670	1.19273	-0.47673	0.06230	-0.42300
Acetone-H <sub>2</sub> O	1.16179	-0.94069	-0.13223	0.05279	1.19165	-0.82978	-0.09977	-0.04018
Methanol-H <sub>2</sub> O	1.07973	0.26490	-0.01904	-0.00674	1.10790	0.29725	-0.01768	-0.07261
Ethanol-H <sub>2</sub> O	1.11565	-0.27405	-0.00615	-0.04271	1.09793	-0.29670	-0.03666	0.00776
NH <sub>3</sub> -H <sub>2</sub> O	1.24890	1.64573	-0.20002	0.04408	1.35090	1.17887	-0.10407	-0.26864



TABLE 4

Comparison of bubble-point calculations by different methods

System	RKS			F-RKS			L-RKS			PR			F-PR			L-PR		
	$\Delta P/\%$	$\Delta y_1$	Rej. <sup>a</sup>	$\Delta P/\%$	$\Delta y_1$	Rej. <sup>a</sup>	$\Delta P/\%$	$\Delta y_1$	Rej. <sup>a</sup>	$\Delta P/\%$	$\Delta y_1$	Rej. <sup>a</sup>	$\Delta P/\%$	$\Delta y_1$	Rej. <sup>a</sup>	$\Delta P/\%$	$\Delta y_1$	Rej. <sup>a</sup>
CH <sub>4</sub> -C <sub>2</sub> H <sub>6</sub>	2.04	0.62	6	2.01	0.39	5	1.39	0.42	6	2.05	0.76	7	1.88	0.29	6	1.36	0.39	7
CH <sub>4</sub> -C <sub>3</sub> H <sub>8</sub>	1.68	1.23	8	1.44	0.99	5	1.15	1.12	7	1.52	1.38	9	1.83	1.32	8	1.16	1.38	8
CH <sub>4</sub> - <i>n</i> -C <sub>4</sub> H <sub>10</sub>	2.62	1.86	0	2.05	1.63	0	1.86	1.83	0	2.55	1.53	0	2.00	1.21	0	2.13	1.38	0
CH <sub>4</sub> - <i>n</i> -C <sub>6</sub> H <sub>14</sub>	2.62	1.45	0	1.85	1.57	0	1.69	1.45	0	2.09	1.38	0	1.70	1.41	0	1.49	1.32	0
CH <sub>4</sub> - <i>n</i> -C <sub>8</sub> H <sub>18</sub>	2.47	0.31	0	1.04	0.20	0	0.90	0.22	0	1.95	0.38	0	1.23	0.29	0	0.89	0.34	0
CH <sub>4</sub> - <i>n</i> -C <sub>10</sub> H <sub>22</sub>	2.43	0.59	2	-	-	-	2.35	0.63	2	2.98	0.34	0	-	-	-	1.78	0.37	0
C <sub>2</sub> H <sub>6</sub> -C <sub>3</sub> H <sub>8</sub>	2.20	1.18	11	1.33	0.78	8	1.60	1.11	11	2.19	1.53	10	2.34	1.52	10	1.91	1.25	10
C <sub>2</sub> H <sub>6</sub> - <i>n</i> -C <sub>5</sub> H <sub>12</sub>	2.01	1.13	0	1.90	0.78	0	2.70	0.87	0	2.29	0.93	0	2.15	0.85	0	2.02	0.90	0
C <sub>2</sub> H <sub>6</sub> - <i>n</i> -C <sub>6</sub> H <sub>14</sub>	11.23	2.26	0	3.96	2.08	0	4.82	2.04	0	11.13	2.37	0	4.44	2.40	0	4.19	2.53	0
C <sub>2</sub> H <sub>6</sub> - <i>n</i> -C <sub>8</sub> H <sub>18</sub>	1.56	0.78	0	1.37	0.77	0	1.44	0.78	0	1.54	0.74	0	1.47	0.75	0	1.48	0.74	0
Average	3.19	1.14		1.88	1.02		1.93	1.05		3.03	1.13		2.12	1.12		1.84	1.06	
CH <sub>4</sub> -CO <sub>2</sub>	2.60	1.06	0	2.56	1.20	0	2.42	1.07	0	2.56	1.08	0	2.99	1.38	0	2.42	0.90	0
CO <sub>2</sub> -C <sub>2</sub> H <sub>6</sub>	0.67	0.51	4	0.59	0.38	2	0.65	0.49	0	1.23	0.56	3	0.70	0.38	3	0.41	0.50	4
C <sub>3</sub> H <sub>8</sub> -CO <sub>2</sub>	1.75	0.52	0	1.41	0.53	0	1.44	0.50	0	1.57	0.50	0	1.46	0.52	0	1.41	0.46	0
CO <sub>2</sub> - <i>n</i> -C <sub>3</sub> H <sub>10</sub>	2.00	1.03	0	0.99	0.78	0	0.84	0.70	0	1.82	0.97	0	1.37	0.85	0	1.26	0.79	0
CO <sub>2</sub> - <i>n</i> -C <sub>5</sub> H <sub>12</sub>	2.45	1.16	8	-	-	-	2.15	1.19	8	2.41	1.30	9	-	-	-	2.14	1.35	9
CO <sub>2</sub> - <i>n</i> -C <sub>6</sub> H <sub>14</sub>	2.21	0.64	0	1.26	0.61	0	0.99	0.60	0	1.99	0.70	0	1.23	0.56	0	1.27	0.60	0
CO <sub>2</sub> - <i>n</i> -C <sub>10</sub> H <sub>22</sub>	3.52	0.92	0	-	-	-	2.58	0.85	0	3.60	0.92	0	-	-	-	2.76	0.90	0
CH <sub>4</sub> -H <sub>2</sub> S	3.29	2.06	3	-	-	-	2.36	1.86	2	3.67	2.17	4	-	-	-	2.80	1.89	3
C <sub>2</sub> H <sub>6</sub> -H <sub>2</sub> S	1.27	1.89	0	-	-	-	1.01	1.98	0	1.27	2.18	0	-	-	-	0.88	2.30	0
H <sub>2</sub> S-C <sub>3</sub> H <sub>8</sub>	2.78	1.75	0	1.96	1.94	0	1.69	1.86	0	2.69	1.71	0	1.92	1.53	0	1.57	1.69	0
H <sub>2</sub> S- <i>n</i> -C <sub>5</sub> H <sub>12</sub>	5.01	1.87	1	2.05	1.68	1	2.67	1.52	0	4.31	1.89	1	2.49	2.02	0	3.26	1.62	0
H <sub>2</sub> S- <i>n</i> -C <sub>10</sub> H <sub>22</sub>	4.68	0.27	0	-	-	-	2.66	0.32	0	4.86	0.36	0	-	-	-	2.17	0.54	0
Average	2.69	1.14		1.55	1.02		1.79	1.08		2.67	1.20		1.74	1.03		1.86	1.13	
CO <sub>2</sub> -methanol	12.10	0.27	0	3.01	0.20	0	2.92	0.13	0	6.99	0.20	0	4.06	0.22	0	3.44	0.20	0
Acetone-CO <sub>2</sub>	0.98	0.27	0	0.84	0.17	0	0.72	0.26	0	1.02	0.19	0	0.86	0.14	0	0.88	0.18	0
Acetone-methanol	2.02	2.14	0	1.82	2.66	0	1.39	2.19	0	2.17	2.05	0	1.79	2.67	0	1.14	2.11	0
Acetone-H <sub>2</sub> O	5.08	3.14	0	3.38	2.44	0	2.40	2.72	0	5.12	3.28	0	3.40	2.48	0	2.49	2.95	0
Methanol-H <sub>2</sub> O	2.22	1.80	0	0.95	1.01	0	1.86	2.11	0	2.35	1.53	0	0.98	0.95	0	1.67	1.76	0
Ethanol-H <sub>2</sub> O	2.12	1.42	3	1.14	1.20	3	1.60	1.29	3	2.08	1.41	4	1.24	1.23	4	1.57	1.24	3
NH <sub>3</sub> -H <sub>2</sub> O	8.52	2.51	0	1.82	1.85	0	3.88	4.39	0	6.95	2.05	0	4.21	2.33	0	4.09	2.58	0
Average	4.71	1.65		1.85	1.36		2.11	1.87		3.81	1.53		2.36	1.43		2.18	1.57	

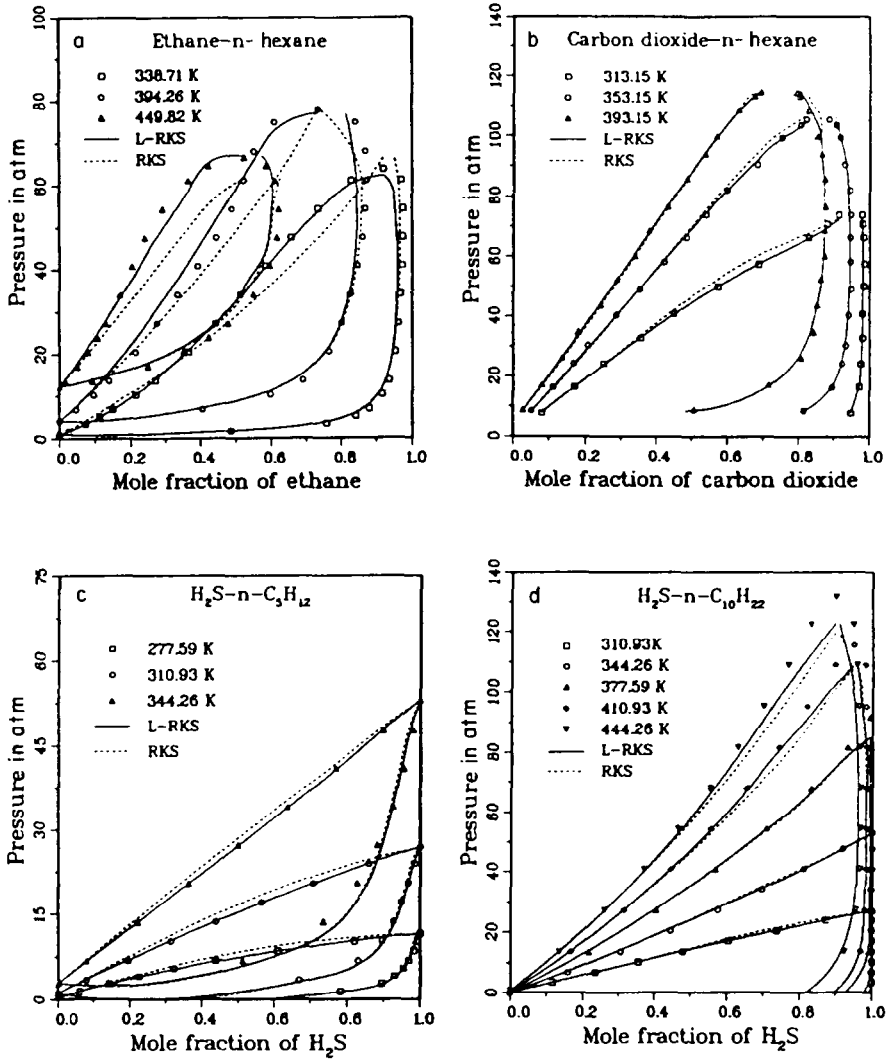


Fig. 2. Comparison of the calculated (L-RKS and RKS) and experimental vapor-liquid equilibria values for (a) ethane-*n*-hexane [25]; (b) carbon dioxide-*n*-hexane [32]; (c) hydrogen sulphide-*n*-pentane [36]; (d) hydrogen sulphide-*n*-decane [37].

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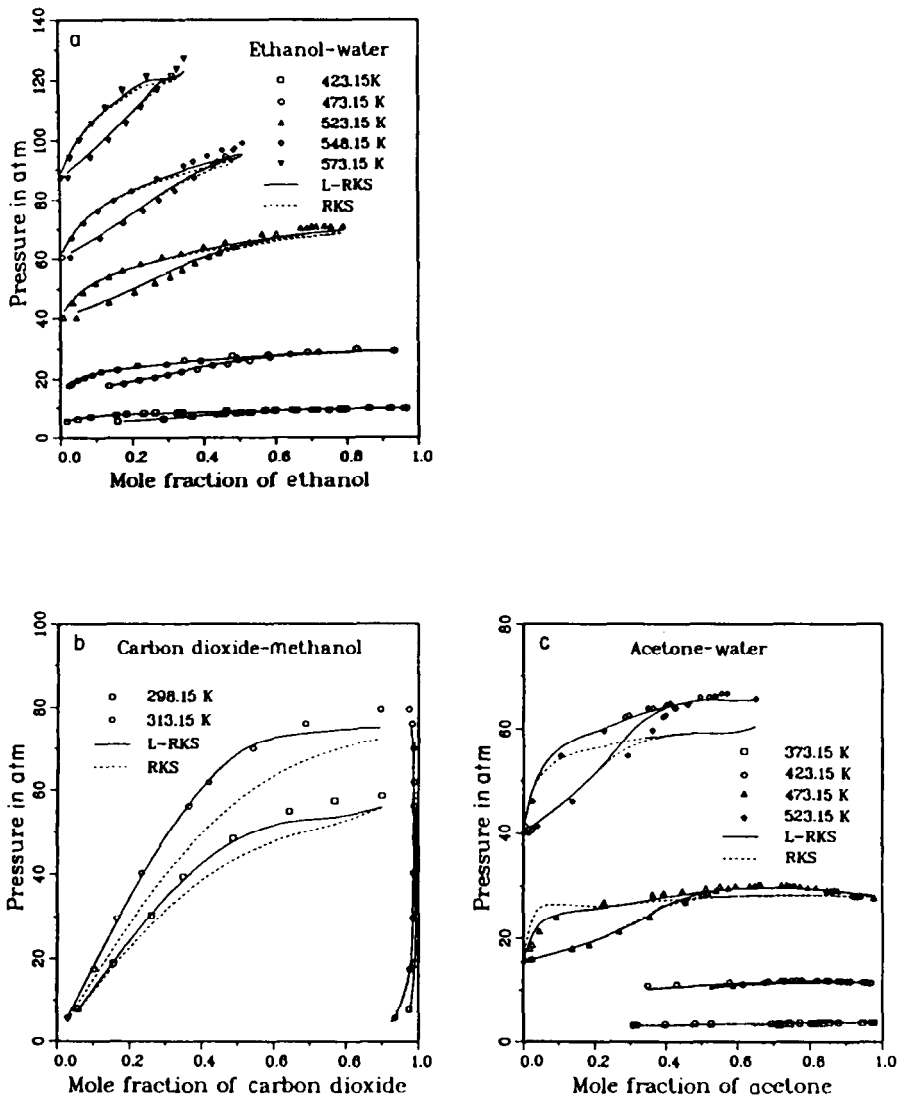


Fig. 3. Comparison of calculated (L-RKS and RKS) and experimental vapor-liquid equilibria values for (a) ethanol-water [41]; (b) carbon dioxide-methanol [38]; (c) acetone-water [40].

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